



CNO Cycle

High mass stars can fuse four hydrogen nuclei into one helium nucleus by a series of nuclear reactions that use carbon, nitrogen, and oxygen as catalysts. This series is known as the CNO cycle. It requires higher temperatures and a large abundance of the catalysts. The sequence of reactions is:

$$\label{eq:constraint} \begin{split} ^{12}\mathrm{C} &+ {}^{1}\mathrm{H} \rightarrow {}^{13}\mathrm{N} + \gamma \\ {}^{13}\mathrm{N} \rightarrow {}^{13}\mathrm{C} + \mathrm{e}^+ + \nu \\ ^{13}\mathrm{C} &+ {}^{1}\mathrm{H} \rightarrow {}^{14}\mathrm{N} + \gamma \\ {}^{14}\mathrm{N} &+ {}^{1}\mathrm{H} \rightarrow {}^{15}\mathrm{O} + \gamma \\ {}^{15}\mathrm{O} \rightarrow {}^{15}\mathrm{N} + \mathrm{e}^+ + \nu \\ {}^{15}\mathrm{N} &+ {}^{1}\mathrm{H} \rightarrow {}^{12}\mathrm{C} + {}^{4}\mathrm{He} \end{split}$$











Energy Released

 $3 {}^{4}\text{He} \rightarrow {}^{12}\text{C}$ $3 {}^{3}\text{m}_{\text{He}} = 3 \times 4.002603 = 12.000781 \text{ u}$ $1 {}^{1}\text{m}_{\text{C}} = 12.000000 \text{ u}$ $\Delta m = 0.000781 \text{ u}$ = 7.27 MeV







Silicon Burning

Assuming that each reaction sequence reaches equilibrium, an "onion-like" shell structure develops. Following C burning, the O in the resulting Ne-O core will ignite, producing a new core composition dominated by Si. Finally, at temperatures near 2.5 billion K, Si burning will begin

²⁸Si + ²⁸Si
$$\rightarrow$$
 ⁵⁶Ni
⁵⁶Ni \rightarrow ⁵⁶Fe via decay

Si burning produces a host of nuclei centered near the Fe peak. Si burning produces an Fe core. Any further reactions that produce nuclei more massive than Fe are endothermic and cannot contribute to the luminosity of the star.











Time Frames

Because C, O, and Si burning produce nuclei with masses progressively nearer the Fe peak of the binding energy curve, less and less energy is generated per gram of fuel. As a result, the time scale for each succeeding reaction sequence becomes shorter.

Evolutionary Stages for $25 \mathcal{M}_{\odot}$ Star

STAGE	CORE (K)	DURATION
Hydrogen burning	$40 \ge 10^{6}$	7,000,000 yr
Helium burning	200 x 10 ⁶	700,000 yr
Carbon burning	600 x 10 ⁶	600 yr
Oxygen burning	1,200 x 10 ⁶	1 yr
Silicon burning	2,700 x 10 ⁶	1 day

The Dilemma

The star is quickly building an Fe core.

But the fusion of Fe will require – not release – energy.

What happens next?

First, the core does become electron degenerate.

Second, ...



Photodisintegration

When the mass of the contracting Fe core has become large enough and the temperature sufficiently high, photodisintegration can, in a very short period of time, undo what the star has been trying to do its entire life – namely, produce elements more massive than H and He.

Of course, this process of stripping Fe down to individual protons and neutrons is highly **endothermic**.

Thermal energy is removed from the gas that would otherwise have resulted in the pressure necessary to support the core of the star.

Creation of Neutrinos

Under the extreme conditions that now exist in the core region (e.g., $T \sim 8$ billion K and $\rho \sim 10$ billion g/cm³ for a 20 solar mass star), the **electrons** that had assisted in supporting the star through pressure **collide with the protons** produced through photodisintegration. That reaction is

 $e^{-}~+~p^{+} \rightarrow n~+~\nu$

The amount of energy that escapes from the star by **neutrino** loss is enormous; during Si burning the **photon** luminosity of a 20 solar mass star is 4.4×10^{31} J/s [= 10,000 L_{sun}],

while the **neutrino** luminosity is $3.1 \ge 10^{38}$ J/s [= 10^{11} L_{sun}].

Core Collapse

Due to (a) the photodisintegration of Fe and (b) electron capture by protons and heavy nuclei,

most of the core's support in the form of electron degeneracy pressure is suddenly gone

and the core begins to collapse extremely rapidly.

Core Collapse

At the radius where the velocity exceeds the local sound speed, the inner core decouples from the now outer core, which is nearly in free-fall.

During the collapse, speeds can reach almost 70,000 km/s (0.25 c), and within about one second a volume the size of the Earth has been compressed to a diameter of 100 km!



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Core collapse	5,400 x 10 ⁶	0.25 seconds	

Suspended Shells

Since mechanical information will only propagate through the star at the speed of sound and because the core collapse proceeds so quickly, there is not enough time for the outer layers to immediately learn about what has happened in the core.

The outer layers, including the O, C, and He shells, as well as the outer envelope, are left in the precarious position of being almost suspended above the catastrophically collapsing core.



Neutron Degeneracy

The collapse of the inner core continues until the density there exceeds about 8 x 10^{14} g/cm³, roughly three times the density of an atomic nucleus.

At that point, the nuclear material that now makes up the inner core stiffens because the **Strong Force** (usually attractive) suddenly becomes repulsive. This is a consequence of the Pauli Exclusion Principle applied to neutrons, e.g., **neutron degeneracy**.

The result is that the extremely-dense and "hard" inner core rebounds somewhat, sending *pressure waves* outward into the in-falling material from the outer core. When the velocity of the pressure waves reach the sound speed, they build into a shock wave.



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Core bounce	23,000 x 10 ⁶	milliseconds	



Shock Wave - Could be Slow

If the initial Fe core is too large, the shock stalls, becoming nearly stationary, with in-falling material accreting onto it. In this case the shock becomes an accretion shock, akin to the situation during protostellar collapse. Below the shock, a **neutrinosphere** develops from the processes of photodisintegration and electron capture.

Since the overlying material is now so dense that even neutrinos cannot easily penetrate it, some of the neutrino energy (\sim 5%) is deposited in the matter just behind the shock. This additional energy heats the material and allows the shock to resume its march toward the surface. The temporary stalling of the shock front is called a *delayed* explosion mechanism.



Neutrino Escape

There is a tremendous production of neutrinos, the majority of which escape into space with a total energy on the order of the binding energy of a neutron star, $\sim 3 \times 10^{47}$ J.

This represents 100 times more energy than the Sun will produce over its entire main-sequence lifetime!

Shock Wave Completion

Meanwhile, the shock wave is still working its way toward the surface, driving the envelope in front of it. The total kinetic energy in the expanding material is on the order of $\sim 1\%$ of the energy liberated in neutrinos.

Finally, when the material becomes transparent at a radius of about 10^{10} km, a tremendous optical display results, releasing $\sim 10^{42}$ J of energy in the form of photons, with a **peak luminosity of nearly roughly** $10^{11} L_{\odot}$, which is comparable to that of an entire galaxy.

This is a **Supernova**.







Final Product

If the initial mass of the star on the main sequence is not too large (< 25 solar masses), the remnant inner core will stabilize and become a **neutron star**, supported by degenerate neutron pressure.

However, if the initial stellar mass is much larger, even the pressure of neutron degeneracy cannot support the remnant against the pull of gravity. The final collapse will produce a **black hole**.