

SOLUTION SET 8

Physics 2022

1. Convert parsecs to light years

$$d = 2000 \text{ pc} \times 3.26 \text{ ly/pc} = 6520 \text{ ly}$$

The supernova was observed in AD 1054. The light began its journey 6520 years before, so the explosion happened in

$$\text{AD } 1054 - 6520 = 5466 \text{ BC}$$

2. $\text{time} = 2012 - 1054 = 958 \text{ years} \times 60 \times 60 \times 24 \times 365.25 = 3.0 \times 10^{10} \text{ s}$

$$\text{radius} = \text{velocity} \times \text{time} = 1450 \text{ km/s} \times (3.0 \times 10^{10} \text{ s})$$

$$= 4.35 \times 10^{13} \text{ km}$$

$$= 2.90 \times 10^5 \text{ AU} = 1.4 \text{ pc} = 4.6 \text{ ly}$$

$$\text{diameter} = 9.2 \text{ ly}$$

3. For a neutron

$$\rho = \mathcal{M} / (4/3 \pi R^3) = 1.7 \times 10^{-27} \text{ kg} / (4/3 \pi (10^{-15} \text{ m})^3) = 4.1 \times 10^{17} \text{ kg/m}^3$$

For a neutron star ($\mathcal{M} = 1.4$ solar masses; $R = 9.7 \text{ km}$)

$$\rho = \mathcal{M} / (4/3 \pi R^3) = 1.4 \times 2.0 \times 10^{30} \text{ kg} / (4/3 \pi (9,700 \text{ m})^3) = 7.3 \times 10^{17} \text{ kg/m}^3$$

- 4a. $\lambda_{\text{max}} = 0.0029 / T = 0.0029 / (3 \times 10^7) = 9.7 \times 10^{-11} \text{ m} = 9.7 \times 10^{-2} \text{ nm}$ (X ray)

- 4b. $L^* = 4 \pi R_*^2 \sigma T_*^4 = 4 \pi (10^4 \text{ m})^2 (5.669 \times 10^{-8}) (3 \times 10^7)^4$

$$= 5.8 \times 10^{31} \text{ W}$$

$$= 5.8 \times 10^{31} / (3.9 \times 10^{26} \text{ W}) = 1.5 \times 10^5 L_{\text{sun}}$$

5. $P = 7.75 \text{ hr} = 8.84 \times 10^{-4} \text{ yr}$
- $a = 2.8 \text{ solar radii} \times (6.96 \times 10^5 \text{ km}) / (1.5 \times 10^8 \text{ km/AU}) = 1.30 \times 10^{-2} \text{ AU}$
- $(\mathcal{M}_1 + \mathcal{M}_2) = a^3 / P^2 = (1.30 \times 10^{-2})^3 / (8.84 \times 10^{-4} \text{ yr})^2 = 2.8 \text{ solar masses}$
6. $R_{\text{sch}} = 2 G \mathcal{M} / c^2 = [2 (6.67 \times 10^{-11}) / (3 \times 10^8 \text{ m/s})^2] \mathcal{M} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}$
- a. $R_{\text{sch}} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}_{\text{earth}} = (1.48 \times 10^{-27} \text{ m/kg}) (5.976 \times 10^{24} \text{ kg})$
- $R_{\text{sch}} = 8.8 \times 10^{-3} \text{ m} = 0.9 \text{ cm}$
- b. $R_{\text{sch}} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}_{\text{saturn}} = (1.48 \times 10^{-27} \text{ m/kg}) (5.685 \times 10^{26} \text{ kg})$
- $R_{\text{sch}} = 8.4 \times 10^{-1} \text{ m} = 84 \text{ cm}$
- c. $R_{\text{sch}} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}_{\text{sun}} = (1.48 \times 10^{-27} \text{ m/kg}) (1.99 \times 10^{30} \text{ kg})$
- $R_{\text{sch}} = 2.95 \times 10^3 \text{ m} = 3 \text{ km}$
7. $R_{\text{sch}} = 2 G \mathcal{M} / c^2 = [2 (6.67 \times 10^{-11}) / (3 \times 10^8 \text{ m/s})^2] \mathcal{M} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}$
- $11 \times 10^3 \text{ m} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}_{\text{sch}}$
- $\mathcal{M}_{\text{sch}} = (11 \times 10^3 \text{ m}) / (1.48 \times 10^{-27} \text{ m/kg})$
- $\mathcal{M}_{\text{sch}} = 7.4 \times 10^{30} \text{ kg} = 3.7 \text{ solar masses}$
8. $R_{\text{sch}} = 2 G \mathcal{M} / c^2 = [2 (6.67 \times 10^{-11}) / (3 \times 10^8 \text{ m/s})^2] \mathcal{M} = (1.48 \times 10^{-27} \text{ m/kg}) \mathcal{M}$
- $R_{\text{sch}} = (1.48 \times 10^{-27} \text{ m/kg}) (8 \mathcal{M}_{\text{sun}}) = (1.48 \times 10^{-27} \text{ m/kg}) (8 \times 1.99 \times 10^{30} \text{ kg})$
- $R_{\text{sch}} = 8 \times 2.95 \times 10^3 \text{ m} = 23.6 \times 10^3 \text{ m} = 23.6 \text{ km}$
- $\rho = \mathcal{M} / (4/3 \pi R^3) = 8 \times 1.99 \times 10^{30} \text{ kg} / (4/3 \pi (23.6 \times 10^3 \text{ m})^3)$
- $= 2.89 \times 10^{17} \text{ kg/m}^3$

Some possibly useful constants

$$1 \text{ pc} = 206,265 \text{ AU} = 3.26 \text{ ly}$$

$$1 \text{ AU} = 1.5 \times 10^8 \text{ km}$$

$$1 \text{ yr} = 3 \times 10^7 \text{ s}$$

$$c = 3 \times 10^8 \text{ m/s}$$

$$\sigma = 5.669 \times 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$$

$$G = 6.7 \times 10^{-11} \text{ N m}^2 / \text{kg}^2$$

$$\mathcal{M}_{\text{sun}} = 2.0 \times 10^{30} \text{ kg}$$

$$R_{\text{sun}} = 6.96 \times 10^5 \text{ km}$$